

**Class XI Session 2024-25**  
**Subject - Mathematics**  
**Sample Question Paper - 10**

**Time Allowed: 3 hours**

**Maximum Marks: 80**

**General Instructions:**

1. This Question paper contains - five sections A, B, C, D and E. Each section is compulsory. However, there are internal choices in some questions.
2. Section A has 18 MCQ's and 02 Assertion-Reason based questions of 1 mark each.
3. Section B has 5 Very Short Answer (VSA)-type questions of 2 marks each.
4. Section C has 6 Short Answer (SA)-type questions of 3 marks each.
5. Section D has 4 Long Answer (LA)-type questions of 5 marks each.
6. Section E has 3 source based/case based/passage based/integrated units of assessment (4 marks each) with sub parts.

**Section A**

1. Find the value of  $\sec\left(\frac{-19\pi}{3}\right)$ . [1]
  - a)  $\frac{1}{2}$
  - b) -2
  - c) 2
  - d)  $\frac{-1}{2}$
2. Number of relations that can be defined on the set  $A = \{a, b, c, d\}$  is [1]
  - a) 24
  - b)  $4^4$
  - c) 16
  - d)  $2^{16}$
3. The mean of five numbers is 30. If one number is excluded, their mean becomes 28. The excluded number is: [1]
  - a) 38
  - b) 30
  - c) 35
  - d) 28
4. If  $f(x) = \frac{x^n - a^n}{x - a}$  for some constant, a, then  $f'(a)$  is equal to [1]
  - a)  $1/2$
  - b) does not exist
  - c) 1
  - d) 0
5. A line passes through P (1, 2) such that its intercept between the axes is bisected at P. The equation of the line is [1]
  - a)  $x + 2y = 5$
  - b)  $2x + y - 4 = 0$
  - c)  $x + y - 3 = 0$
  - d)  $x - y + 1 = 0$
6. Distance of the point  $(\alpha, \beta, \gamma)$  from y-axis is [1]
  - a)  $\sqrt{\alpha^2 + \gamma^2}$
  - b)  $|\beta| + |\gamma|$

- c)  $|\beta|$  d)  $\beta$
7. Mark the correct answer for  $(1 + i)^{-1} = ?$  [1]  
 a)  $\left(\frac{-1}{2} + \frac{1}{2}i\right)$  b)  $(2 - 3i)$   
 c)  $\left(\frac{1}{2} - \frac{1}{2}i\right)$  d)  $(2 - i)$
8. If  ${}^{20}C_{r+1} = {}^{20}C_{r-1}$ , then r is equal to [1]  
 a) 19 b) 10  
 c) 12 d) 11
9. If  $y = \frac{1 + \frac{1}{x^2}}{1 - \frac{1}{x^2}}$  then  $\frac{dy}{dx}$  is equal to [1]  
 a)  $\frac{-4x}{x^2-1}$  b)  $\frac{1-x^2}{4x}$   
 c)  $\frac{-4x}{(x^2-1)^2}$  d)  $\frac{4x}{x^2-1}$
10. Which is smaller,  $\sin 64^\circ$  or  $\cos 64^\circ$ ? [1]  
 a)  $\cos 64^\circ$  b)  $\sin 64^\circ$   
 c) cannot be compared d) both are equal
11. Let  $F_1$  be the set of parallelograms,  $F_2$  the set of rectangles,  $F_3$  the set of rhombuses,  $F_4$  the set of squares and  $F_5$  the set of trapeziums in a plane. Then  $F_1$  may be equal to [1]  
 a)  $F_2 \cap F_3$  b)  $F_3 \cap F_4$   
 c)  $F_2 \cup F_5$  d)  $F_2 \cup F_3 \cup F_4 \cup F_1$
12.  $\left\{ \frac{c_1}{c_0} + 2\frac{C_2}{C_1} + 3\frac{C_3}{C_2} + \dots + n \cdot \frac{C_n}{C_{n-1}} \right\} = ?$  [1]  
 a)  $\frac{1}{2}n(n+1)$  b)  $2n$   
 c)  $2^{n-1}$  d)  $2^n$
13.  $(\sqrt{5} + 1)^4 + (\sqrt{5} - 1)^4$  is [1]  
 a) an irrational number b) a negative real number  
 c) a rational number d) a negative integer
14. The solution set of  $6x - 1 > 5$  is : [1]  
 a)  $\{x : x > 1, x \in \mathbb{N}\}$  b)  $\{x : x > 1, x \in \mathbb{R}\}$   
 c)  $\{x : x < 1, x \in \mathbb{N}\}$  d)  $\{x : x < 1, x \in \mathbb{W}\}$
15. If  $A = \{1, 3, 5, B\}$  and  $B = \{2, 4\}$ , then [1]  
 a)  $\{4\} \subset A$  b) None of these  
 c)  $B \subset A$  d)  $4 \in A$
16. The value of  $\frac{2(\sin 2x + 2\cos^2 x - 1)}{\cos x - \sin x - \cos 3x + \sin 3x}$  is [1]  
 a)  $\sin x$  b)  $\cos x$   
 c)  $\operatorname{cosec} x$  d)  $\sec x$

[1]



fourth vertex.

28. Using binomial theorem, expand:  $(x^2 - \frac{2}{x})^7$ . [3]

OR

Show that  $2^{4n+4} - 15n - 16$  where  $n \in \mathbf{N}$  is divisible by 225

29. Find the derivative of  $x^{-4}(3 - 4x^{-5})$  [3]

OR

Find the derivative of  $\frac{(x-1)(x-2)}{(x-3)(x-4)}$ .

30. If the AM and GM of two positive numbers a and b are in the ratio m : n, show that [3]

$$a : b = (m + \sqrt{m^2 - n^2}) : (m - \sqrt{m^2 - n^2})$$

OR

Evaluate:  $\sum_{k=1}^{11} (2 + 3^k)$

31. In a class, 18 students took Physics, 23 students took Chemistry and 24 students took [3]

Mathematics of these 13 took both Chemistry and Mathematics, 12 took both Physics and Chemistry and 11 took both Physics and Mathematics. If 6 students offered all the three subjects, find:

i. The total number of students.

ii. How many took Maths but not Chemistry.

iii. How many took exactly one of the three subjects.

#### Section D

32. Find the mean deviation about the mean for the following data: [5]

$x_i$	3	5	7	9	11	13
$f_i$	6	8	15	3	8	4

33. Find the equation of a circle concentric with the circle  $x^2 + y^2 + 4x + 6y + 11 = 0$  and passing through the point (5, 4). [5]

OR

Find the equation of the hyperbola, the length of whose latus rectum is 4 and the eccentricity is 3.

34. Solve the following system of linear inequalities [5]

$$\frac{4x}{3} - \frac{9}{4} < x + \frac{3}{4} \text{ and } \frac{7x-1}{3} - \frac{7x+2}{6} > x.$$

35. Prove that:  $\sin 20^\circ \sin 40^\circ \sin 80^\circ = \frac{\sqrt{3}}{8}$  [5]

OR

Prove that  $\cos 12^\circ + \cos 60^\circ + \cos 84^\circ = \cos 24^\circ + \cos 48^\circ$

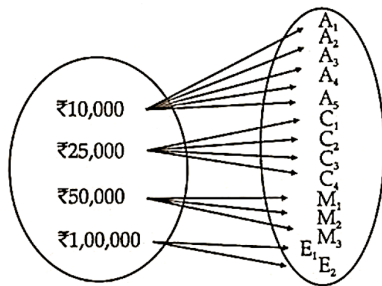
#### Section E

36. Read the following text carefully and answer the questions that follow: [4]

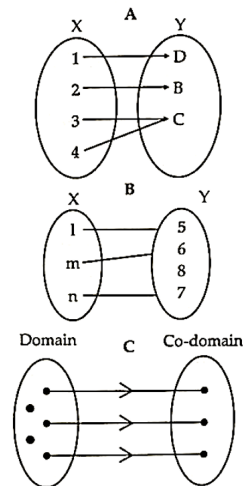
A Relation R from A to B can be depicted pictorially using arrow diagram. In arrow diagram, we write down the elements of two sets A and B in two disjoint circles. Then we draw arrow from set A to set B whenever  $(A, B) \in R$ . An example of information depicted through an arrow diagram is shown below. For example:

A company has four categories of employees given by Assistants (A), Clerks (C), Managers (M) and an Executive Officer (E). The company provides ₹ 10,000, ₹ 25,000, ₹ 50,000 and ₹ 1,00,000 to the people who work in the categories A, C, M and E respectively. Here  $A_1, A_2, A_3, A_4$  and  $A_5$  are Assistants;  $C_1, C_2, C_3, C_4$  are Clerks;  $M_1, M_2, M_3$  are Managers and  $E_1, E_2$  are Executive Officers then the relation R is defined by  $xRy$ ,

where  $x$  is the salary given to person  $y$ .

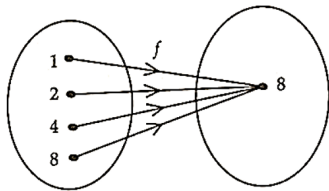


- i. If the number of elements in set A and set B are  $p$  and  $q$  then find the number of functions from A to B. (1)
- ii. If the number of elements in set A and set B are  $p$  and  $q$ , then find the number of relations from A to B. (1)
- iii. Which figures shows a relation between the two non-empty sets? (2)



**OR**

Show the relation defined in the below arrow diagram from set A to set B. (2)



37. **Read the following text carefully and answer the questions that follow:** [4]

There are 4 red, 5 blue and 3 green marbles in a basket.

- i. If two marbles are picked at randomly, find the probability that both red marbles. (1)
- ii. If three marbles are picked at randomly, find the probability that all green marbles. (1)
- iii. If two marbles are picked at randomly then find the probability that both are not blue marbles. (2)

**OR**

If three marbles are picked at randomly, then find the probability that atleast one of them is blue. (2)

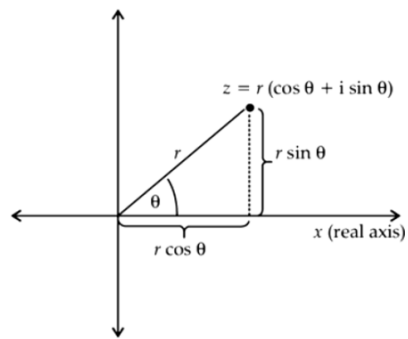
38. **Read the following text carefully and answer the questions that follow:** [4]

Consider the complex number  $Z = 2 - 2i$ .

## Complex Number in Polar Form

### Complex Numbers in Polar Form

$i$  (imaginary axis)



- Find the principal argument of  $Z$ . (1)
- Find the value of  $\mathbf{z\bar{z}}$ ? (1)
- Find the value of  $|Z|$ . (2)

**OR**

Find the real part of  $Z$ . (2)

# Solution

## Section A

1. (c) 2  
**Explanation:**  $\sec\left(\frac{-19\pi}{3}\right) = \sec\frac{19\pi}{3} [\because \sec(-\theta) = \sec\theta]$   
 $= \sec\left(6\pi + \frac{\pi}{3}\right) = \sec\frac{\pi}{3} = 2 [\because \sec(2n\pi + \theta) = \sec\theta]$
2. (d)  $2^{16}$   
**Explanation:** No. of elements in the set  $A = 4$ . Therefore, the no. of elements in  $A \times A = 4 \times 4 = 16$ . As, the no. of relations in  $A \times A =$  no. of subsets of  $A \times A = 2^{16}$ .
3. (a) 38  
**Explanation:** Let the numbers are  $x_1, x_2, x_3, x_4$  and  $x_5$ . Then,  
we have,  $\frac{x_1 + x_2 + x_3 + x_4 + x_5}{5} = 30$   
 $\Rightarrow x_1 + x_2 + x_3 + x_4 + x_5 = 150 \dots(i)$   
Now, suppose  $x_1$  is excluded, then  $\frac{x_2 + x_3 + x_4 + x_5}{4} = 28$  [given]  
 $\Rightarrow x_2 + x_3 + x_4 + x_5 = 112 \dots(ii)$   
From Eqs. (i) and (ii), we get  $x_1 = 150 - 112 = 38$
4. (b) does not exist  
**Explanation:** Given  $f(x) = \frac{x^n - a^n}{x - a}$   
 $f'(x) = \frac{(x-a)(n \cdot x^{n-1}) - (x^n - a^n) \cdot 1}{(x-a)^2}$   
 $\therefore f'(a) = \frac{(a-a)(n \cdot a^{n-1}) - (a^n - a^n)}{(a-a)^2}$   
So  $f'(a) = \frac{0}{0} =$  does not exist
5. (b)  $2x + y - 4 = 0$   
**Explanation:** We know that the equation of a line making intercepts  $a$  and  $b$  with  $x$ -axis and  $y$ -axis, respectively, is given by  $\frac{x}{a} + \frac{y}{b} = 1$   
Here we have  $1 = \frac{a+0}{2}$  and  $2 = \frac{0+b}{2}$   
which give  $a = 2$  and  $b = 4$ .  
Thus, now we have to find the required equation of the line is given by  $\frac{x}{2} + \frac{y}{4} = 1$  or  $2x + y - 4 = 0$
6. (a)  $\sqrt{\alpha^2 + \gamma^2}$   
**Explanation:** The foot of perpendicular from point  $P(\alpha, \beta, \gamma)$  on  $y$ -axis is  $Q(0, \beta, 0)$   
 $\therefore$  Required distance,  $PQ = \sqrt{(\alpha - 0)^2 + (\beta - \beta)^2 + (\gamma - 0)^2} = \sqrt{\alpha^2 + \gamma^2}$
7. (c)  $\left(\frac{1}{2} - \frac{1}{2}i\right)$   
**Explanation:**  $(1+i)^{-1} = \frac{1}{(1+i)} = \frac{1}{(1+i)} \times \frac{(1-i)}{(1-i)} = \frac{(1-i)}{(1-i)^2} = \frac{(1-i)}{2} = \left(\frac{1}{2} - \frac{1}{2}i\right)$
8. (b) 10  
**Explanation:**  $r + 1 + r - 1 = 20$  [ $\because {}^n C_x = {}^n C_y \Rightarrow n = x + y$  or  $x = y$ ]  
 $\Rightarrow 2r = 20$   
 $\Rightarrow r = 10$ .

9.

(c)  $\frac{-4x}{(x^2-1)^2}$

**Explanation:** Given  $y = \frac{1+\frac{1}{x^2}}{1-\frac{1}{x^2}} \Rightarrow y = \frac{x^2+1}{x^2-1}$

$$\begin{aligned} \therefore \frac{dy}{dx} &= \frac{(x^2-1) \cdot 2x - (x^2+1) \cdot 2x}{(x^2-1)^2} \\ &= \frac{2x(x^2-1-x^2-1)}{(x^2-1)^2} = \frac{2x(-2)}{(x^2-1)^2} = \frac{-4x}{(x^2-1)^2} \end{aligned}$$

10. (a)  $\cos 64^\circ$

**Explanation:** In quadrant I,  $\sin \theta$  is increasing.

Now,  $\cos 64^\circ = \cos (90^\circ - 26^\circ) = \sin 26^\circ$ .

Clearly,  $\sin 26^\circ < \sin 64^\circ \Rightarrow \cos 64^\circ < \sin 64^\circ$

11.

(d)  $F_2 \cup F_3 \cup F_4 \cup F_1$

**Explanation:** We know that

Every rectangle, square and rhombus is a parallelogram

But, no trapezium is a parallelogram

Thus,  $F_1 = F_2 \cup F_3 \cup F_4 \cup F_1$

12. (a)  $\frac{1}{2}n(n+1)$

**Explanation:** We know that  $\frac{C_r}{C_{r-1}} = \frac{n-r+1}{r}$ ,

Substituting  $r = 1, 2, 3, \dots, n$ , we obtain

$$\frac{C_1}{C_0} + 2 \cdot \frac{C_2}{C_1} + 3 \cdot \frac{C_3}{C_2} + \dots + n \cdot \frac{C_n}{C_{n-1}} = n + (n-1) + (n-2) + \dots + 1 = \frac{1}{2}n(n+1).$$

13.

(c) a rational number

**Explanation:** We have  $(a+b)^n + (a-b)^n$

$$\begin{aligned} &= [{}^n C_0 a^n + {}^n C_1 a^{n-1} b + {}^n C_2 a^{n-2} b^2 + {}^n C_3 a^{n-3} b^3 + \dots + {}^n C_n b^n] + \\ &[{}^n C_0 a^n - {}^n C_1 a^{n-1} b + {}^n C_2 a^{n-2} b^2 - {}^n C_3 a^{n-3} b^3 + \dots + (-1)^n \cdot {}^n C_n b^n] \\ &= 2[{}^n C_0 a^n + {}^n C_2 a^{n-2} b^2 + \dots] \end{aligned}$$

Let  $a = \sqrt{5}$  and  $b = 1$  and  $n = 4$

$$\begin{aligned} \text{Now we get } &(\sqrt{5} + 1)^4 + (\sqrt{5} - 1)^4 = 2 [{}^4 C_0 (\sqrt{5})^4 + {}^4 C_2 (\sqrt{5})^2 1^2 + {}^4 C_4 (\sqrt{5})^0 1^4] \\ &= 2[25 + 30 + 1] = 112 \end{aligned}$$

14.

(b)  $\{x : x > 1, x \in \mathbb{R}\}$

**Explanation:**  $6x - 1 > 5$

$$\Rightarrow 6x - 1 + 1 > 5 + 1$$

$$\Rightarrow 6x > 6$$

$$\Rightarrow x > 1$$

Hence the solution set is  $\{x : x > 1, x \in \mathbb{R}\}$

15.

(b) None of these

**Explanation:**  $4 \notin A$

$\{4\} \not\subset A$

$B \not\subset A$

Therefore, we can say that none of these options satisfy the given relation.

16.

(c)  $\operatorname{cosec} x$

**Explanation:** We have,

$$\begin{aligned} &\frac{2(\sin 2x + 2 \cos^2 x - 1)}{\cos x - \sin x - \cos 3x + \sin 3x} \\ &= \frac{2(\sin 2x + \cos 2x)}{\cos x - \sin x - 4 \cos^3 x + 3 \cos x + 3 \sin x - 4 \sin^3 x} \end{aligned}$$



$$\begin{aligned}
&= \frac{2(\sin 2x + \cos 2x)}{4 \cos x - 4 \cos^3 x + 2 \sin x - 4 \sin^3 x} \\
&= \frac{2(\sin 2x + \cos 2x)}{2(\sin 2x + \cos 2x)} \\
&= \frac{4 \cos x (1 - \cos^2 x) + 2 \sin x (1 - 2 \sin^2 x)}{2(\sin 2x + \cos 2x)} \\
&= \frac{4 \cos x \sin^2 x + 2 \sin x \cos 2x}{2(\sin 2x + \cos 2x)} \\
&= \frac{2 \times 2 \sin x \cos x \sin x + 2 \sin x \cos 2x}{2(\sin 2x + \cos 2x)} \\
&= \frac{2 \sin 2x \sin x + 2 \sin x \cos 2x}{2(\sin 2x + \cos 2x)} \\
&= \frac{2 \sin x (\sin 2x + \cos 2x)}{2(\sin 2x + \cos 2x)} \\
&= \frac{1}{\sin x} \\
&= \operatorname{cosec} x
\end{aligned}$$

17.

(d) None of these

**Explanation:**  $\lim_{x \rightarrow 3} \frac{x-3}{|x-3|}$

LHL at  $x = 3$

$$\lim_{x \rightarrow 3^-} \frac{x-3}{-(x-3)} \quad [\because |x-3| = -(x-3) \text{ when } x < 3]$$

$$= -1$$

RHL at  $x = 3$

$$\lim_{x \rightarrow 3^+} \frac{x-3}{x-3} \quad [\because |x-3| = x-3, \text{ when } x > 3]$$

$$= 1$$

LHL  $\neq$  RHL

18.

(c) 60

**Explanation:** Required number of ways =  ${}^5P_3 = \frac{5!}{(5-3)!} = \frac{5 \times 4 \times 3 \times 2 \times 1}{2 \times 1} = 60$

19.

(b) Both A and R are true but R is not the correct explanation of A.

**Explanation: Assertion:** We know that, a set which is empty or consists of a definite number of elements, is called finite, otherwise the set is called infinite. Since, set A contains finite number of elements. So, it is a finite set.

**Reason:** We do not know the number of elements in B, but it is some natural number. So, B is also finite.

20. (a) Both A and R are true and R is the correct explanation of A.

**Explanation: Assertion:** If  $\frac{-2}{7}$ ,  $k$ ,  $\frac{-7}{2}$  are in G.P.

$$\text{Then, } \frac{a_2}{a_1} = \frac{a_3}{a_2}$$

$$[\because \text{common ratio (r)} = \frac{a_2}{a_1} = \frac{a_3}{a_2} = \frac{a_4}{a_3} = \dots]$$

$$\therefore \frac{k}{\frac{-2}{7}} = \frac{\frac{-7}{2}}{k}$$

$$\Rightarrow \frac{7}{-2} k = \frac{-7}{2} \times \frac{1}{k}$$

$$\Rightarrow 7k \times 2k = -7 \times (-2)$$

$$\Rightarrow 14k^2 = 14$$

$$\Rightarrow k^2 = 1 \Rightarrow k = \pm 1$$

Hence, Assertion and Reason both are true and Reason is the correct explanation of Assertion.

### Section B

21. i. Here we have,  $\{(x, x^2) : x \text{ is a prime number less than } 10\}$ .

Roster form of  $R = \{(1, 1), (2, 4), (3, 9), (5, 25), (7, 49)\}$

ii. The domain of  $R$  is the set of first co-ordinates of  $R$

Domain of  $R = \{1, 2, 3, 5, 7\}$

The domain of  $R$  is the set of first co-ordinates of  $R$

Range( $R$ ) =  $\{1, 4, 9, 25, 49\}$

OR

Here  $R = \{(a, b) : a, b \in N \text{ and } a = b^2\}$

(i) No  $(3, 3) \in R$  because  $3 \neq 3^2$

(ii) No.  $(9, 3) \in R$  but  $(3, 9) \in R$

(iii) No.  $(81, 9) \in R$   $(9, 3) \in R$  but  $(81, 3) \notin R$

22. To find: Differentiation of  $(x^2 - 4x + 5)(x^3 - 2)$

Formula used: (i)  $(uv)' = u'v + uv'$  (Using Leibnitz or product rule)

(ii)  $\frac{dx^n}{dx} = nx^{n-1}$

Let  $u = (x^2 - 4x + 5)$  and  $v = (x^3 - 2)$

$$u' = \frac{du}{dx} = \frac{d(x^2 - 4x + 5)}{dx} = 2x - 4$$

$$v' = \frac{dv}{dx} = \frac{d(x^3 - 2)}{dx} = 3x^2$$

Put the above obtained values in the formula:-

$$(uv)' = u'v + uv'$$

$$[(x^2 - 4x + 5)(x^3 - 2)]' = (2x - 4)(x^3 - 2) + (x^2 - 4x + 5)(3x^2)$$

$$= 2x^4 - 4x - 4x^3 + 8 + 3x^4 - 12x^3 + 15x^2$$

$$= 5x^4 - 16x^3 + 15x^2 - 4x + 8.$$

23. i. We know that,

If odds in favor of the occurrence an event are a:b, then the probability of an event to occur is  $\frac{a}{a+b}$

Given, probability =  $\frac{5}{14}$

We know, probability of an event to occur =  $\frac{a}{a+b}$

Here, a = 5 and a + b = 14 i.e. b = 9

So,  $\frac{a}{a+b} = \frac{5}{14}$

odds in favor of its occurrence = a : b = 5 : 9

Conclusion: Odds in favor of its occurrence is 5 : 9

ii. As we solved in part (i), a = 5 and b = 9

Also, we know, odds against its occurrence is b : a = 9 : 5

Conclusion: Odds against its occurrence is 9 : 5

OR

We have given that:  $P(A) = 0.60$ ,  $P(A \text{ or } B) = 0.85$  and  $P(A \text{ and } B) = 0.42$

To find :  $P(B)$

Formula used :  $P(A \text{ or } B) = P(A) + P(B) - P(A \text{ and } B)$

Substituting the values in the above formula we get,

$$0.85 = 0.60 + P(B) - 0.42$$

$$0.85 = 0.18 + P(B)$$

$$0.85 - 0.18 = P(B)$$

$$0.67 = P(B)$$

$$P(B) = 0.67$$

24. We have,  $B = \{x : x^2 + 2x + 1 = 0, x \in N\}$

Now,  $x^2 + 2x + 1 = 0$

$$\Rightarrow (x + 1)^2 = 0$$

$\Rightarrow x = -1$  which is not a natural number.

Thus,  $B = \{\} = \phi$

Hence, B is not a singleton set.

25. Let the point on the y-axis be  $P(0, y)$

Here, it is given that P is equidistant from  $A(-4, 3)$  and  $B(5, 2)$ .

i.e.,  $PA = PB$

$$\Rightarrow \sqrt{(-4 - 0)^2 + (3 - y)^2} = \sqrt{(5 - 0)^2 + (2 - y)^2}$$

Squaring both sides, we obtain

$$\Rightarrow (-4 - 0)^2 + (3 - y)^2 = (5 - 0)^2 + (2 - y)^2$$

$$\Rightarrow 16 + 9 - 6y + y^2 = 25 + 4 - 4y + y^2$$

$$\Rightarrow 25 - 6y = 29 - 4y$$

$$\Rightarrow 2y = -4$$

$$\Rightarrow y = -2$$

Thus, the required point on the y-axis is (0, -2).

### Section C

26. Here  ${}^{22}P_{r+1} : {}^{20}P_{r+2} = 11 : 52$

$$\Rightarrow \frac{22!}{(21-r)!} \times \frac{(18-r)!}{20!} = \frac{11}{52}$$

$$\Rightarrow \frac{22 \times 21 \times 20!}{(21-r)(20-r)(19-r)(18-r)!} \times \frac{(18-r)!}{20!} = \frac{11}{52}$$

$$\Rightarrow \frac{22 \times 21}{(21-r)(20-r)(19-r)} = \frac{11}{52}$$

$$\Rightarrow (21-r)(20-r)(19-r) = 2 \times 21 \times 52$$

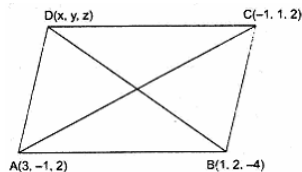
$$\Rightarrow (21-r)(20-r)(19-r) = 14 \times 13 \times 12$$

$$\Rightarrow (21-r)(20-r)(19-r) = (21-7)(20-7)(19-7)$$

$$\Rightarrow r = 7$$

27. Let D (x, y, z) be the fourth vertex of parallelogram ABCD.

We know that diagonals of a parallelogram bisect each other. So the mid points of AC and BD coincide.



$$\therefore \text{Coordinates of mid point of AC} \left( \frac{3-1}{2}, \frac{-1+1}{2}, \frac{2+2}{2} \right)$$

$$= (1, 0, 2)$$

$$\text{Also coordinates of mid point of BD} \left( \frac{x+1}{2}, \frac{y+2}{2}, \frac{z-4}{2} \right)$$

$$\therefore \frac{x+1}{2} = 1 \Rightarrow x+1=2 \Rightarrow x=1$$

$$\frac{y+2}{2} = 0 \Rightarrow y+2=0 \Rightarrow y=-2$$

$$\frac{z-4}{2} = 2 \Rightarrow z-4=4 \Rightarrow z=8$$

Thus the coordinates of point D are (1, -2, 8)

28. To find: Expansion of  $\left(x^2 - \frac{3x}{7}\right)^7$

$$\text{Formula used: } {}^nC_r = \frac{n!}{(n-r)!r!}$$

$$\text{We know that, } (a+b)^n = {}^nC_0 a^n + {}^nC_1 a^{n-1}b + {}^nC_2 a^{n-2}b^2 + \dots + {}^nC_{n-1} a b^{n-1} + {}^nC_n b^n$$

$$\text{Here We have, } \left(x^2 - \frac{3x}{7}\right)^7$$

$$\Rightarrow \left[ {}^7C_0 (x^2)^{7-0} \right] + \left[ {}^7C_1 (x^2)^{7-1} \left(-\frac{3x}{7}\right)^1 \right] + \left[ {}^7C_2 (x^2)^{7-2} \left(-\frac{3x}{7}\right)^2 \right] + \left[ {}^7C_3 (x^2)^{7-3} \left(-\frac{3x}{7}\right)^3 \right] + \left[ {}^7C_4 (x^2)^{7-4} \left(-\frac{3x}{7}\right)^4 \right]$$

$$+ \left[ {}^7C_5 (x^2)^{7-5} \left(-\frac{3x}{7}\right)^5 \right] + \left[ {}^7C_6 (x^2)^{7-6} \left(-\frac{3x}{7}\right)^6 \right] + \left[ {}^7C_7 \left(-\frac{3x}{7}\right)^7 \right]$$

$$\Rightarrow \left[ \frac{7!}{0!(7-0)!} (x^2)^7 \right] - \left[ \frac{7!}{1!(7-1)!} (x^2)^6 \left(\frac{3x}{7}\right) \right] + \left[ \frac{7!}{2!(7-2)!} (x^2)^5 \left(\frac{9x^2}{49}\right) \right] - \left[ \frac{7!}{3!(7-3)!} (x^2)^4 \left(\frac{27x^3}{343}\right) \right]$$

$$+ \left[ \frac{7!}{4!(7-4)!} (x^2)^3 \left(\frac{81x^4}{2401}\right) \right] - \left[ \frac{7!}{5!(7-5)!} (x^2)^2 \left(\frac{243x^5}{16807}\right) \right] + \left[ \frac{7!}{6!(7-6)!} (x^2)^1 \left(\frac{729x^6}{117649}\right) \right] - \left[ \frac{7!}{7!(7-7)!} \left(\frac{2187x^7}{823543}\right) \right]$$

$$- \left[ \frac{7!}{7!(7-7)!} \left(\frac{2187x^7}{823543}\right) \right] + \left[ 21 (x^{10}) \left(\frac{9x^2}{49}\right) \right] - \left[ 35 (x^8) \left(\frac{27x^3}{343}\right) \right]$$

$$+ \left[ 35 (x^6) \left(\frac{81x^4}{2401}\right) \right] - \left[ 21 (x^4) \left(\frac{243x^5}{16807}\right) \right] + \left[ 7 (x^2) \left(\frac{729x^6}{117649}\right) \right] - \left[ 1 \left(\frac{2187x^7}{823543}\right) \right]$$

$$\Rightarrow x^{24} - 3x^{13} + \left(\frac{27}{7}\right)x^{12} - \left(\frac{135}{49}\right)x^{11} + \left(\frac{405}{343}\right)x^{10} - \left(\frac{729}{2401}\right)x^9 + \left(\frac{729}{16807}\right)x^8 - \left(\frac{2187}{823543}\right)x^7$$

$$x^{14} - 3x^{13} + \left(\frac{27}{7}\right)x^{12} - \left(\frac{135}{49}\right)x^{11} + \left(\frac{405}{343}\right)x^{10} - \left(\frac{729}{2401}\right)x^9 + \left(\frac{729}{16807}\right)x^8 - \left(\frac{2187}{823543}\right)x^7$$

OR

$$\text{From the given equation we have } 2^{4n+4} - 15n - 16 = 2^{4(n+1)} - 15n - 16$$

$$= 16^{n+1} - 15n - 16$$

$$= (1+15)^{n+1} - 15n - 16$$

Using binomial expression we have

$$= {}^{n+1}C_0 15^0 + {}^{n+1}C_1 15^1 + {}^{n+1}C_2 15^2 + \dots + {}^{n+1}C_3 15^3$$

$$+ \dots + x + [C], (15)^{n+1} - 15n - 16$$

$$= 1 + (n+1)15 + {}^{n+1}C_2 15^2 + {}^{n+1}C_3 15^3$$

$$\begin{aligned}
& + \dots + n + 1 C_{n+1} (15)^{n+1} - 15n - 16 \\
& = 1 + 15n + 15^{n+1} C_2 15^2 +^{n+1} C_3 15 \\
& + \dots +^{n+1} C_{n+1} (15)^{n+1} - 15n - 16 \\
& = 15^2 [^{n+1} C_2 +^{n+1} C_3 15 + \dots \text{so on}] \\
& \text{Thus, } 2^{4n+4} - 15n - 16 \text{ is divisible 225.}
\end{aligned}$$

29. Here  $f(x) = x^{-4} (3 - 4x^{-5})$

$$\begin{aligned}
f'(x) &= \frac{d}{dx} [x^{-4} (3 - 4x^{-5})] \\
&= x^{-4} \frac{d}{dx} (3 - 4x^{-5}) + (3 - 4x^{-5}) \frac{d}{dx} (x^{-4}) \\
&= x^{-4} (20x^{-6}) + (3 - 4x^{-5}) (-4x^{-5}) \\
&= 20x^{-10} - 12x^{-5} + 16x^{-10} \\
&= 36x^{-10} - 12x^{-5} = \frac{36}{x^{10}} - \frac{12}{x^5}
\end{aligned}$$

OR

Let  $y = \frac{(x-1)(x-2)}{(x-3)(x-4)}$

On differentiating both sides w.r.t. x, we get

$$\begin{aligned}
\frac{dy}{dx} &= \frac{\left[ \frac{(x-3)(x-4)}{dx} [(x-1)(x-2)] - (x-1) \right]}{\left[ \frac{(x-2)}{dx} [(x-3)(x-4)] \right]} \\
&= \frac{\left[ \frac{d}{dx} \left( \frac{u}{v} \right) = \frac{v \frac{du}{dx} - u \frac{dv}{dx}}{v^2} \right]}{\left[ \frac{(x-3)(x-4)}{dx} [(x-1)(x-2)] + (x-2) \frac{d}{dx} (x-1) \right] - (x-1)(x-2) \left[ \frac{(x-3)}{dx} (x-4) + (x-4) \frac{d}{dx} (x-3) \right]} \\
&= \frac{(x-3)(x-4) [(x-1) \cdot 1 + (x-2) \cdot 1] - (x-1)(x-2) [(x-3) \cdot 1 + (x-4) \cdot 1]}{(x-3)^2 (x-4)^2} \\
&= \frac{(x-3)(x-4) [2x-3] - (x-1)(x-2) [2x-7]}{(x-3)^2 (x-4)^2} \\
&= \frac{(x^2 - 7x + 12)(2x-3) - (x^2 - 3x + 2)(2x-7)}{(x-3)^2 (x-4)^2} \\
&= \frac{2x^3 - 14x^2 + 24x - 3x^2 + 21x - 36 - 2x^3 + 6x^2 - 4x + 7x^2 - 21x + 14}{(x-3)^2 (x-4)^2} \\
&= \frac{-4x^2 + 20x - 22}{(x-3)^2 (x-4)^2}
\end{aligned}$$

30.  $\frac{a+b}{\frac{2}{\sqrt{ab}}} = \frac{m}{n}$   
 $\frac{a+b}{2\sqrt{ab}} = \frac{m}{n}$

By C and D

$$\begin{aligned}
\frac{a+b+2\sqrt{ab}}{a+b-2\sqrt{ab}} &= \frac{m+n}{m-n} \\
\frac{(\sqrt{a}+\sqrt{b})^2}{(\sqrt{a}-\sqrt{b})^2} &= \frac{m+n}{m-n} \\
\frac{\sqrt{a}+\sqrt{b}}{\sqrt{a}-\sqrt{b}} &= \frac{\sqrt{m+n}}{\sqrt{m-n}}
\end{aligned}$$

By C and D

$$\frac{\sqrt{a}}{\sqrt{b}} = \frac{\sqrt{m+n} + \sqrt{m-n}}{\sqrt{m+n} - \sqrt{m-n}}$$

Squaring both side

$$\begin{aligned}
\frac{a}{b} &= \frac{m+n+m-n+2\sqrt{m^2-n^2}}{m+n+m-n-2\sqrt{m^2-n^2}} \\
\frac{a}{b} &= \frac{m+\sqrt{m^2-n^2}}{m-\sqrt{m^2-n^2}}
\end{aligned}$$

OR

Given:  $\sum_{k=1}^{11} (2 + 3^k)$

$$\begin{aligned}
&= (2 + 3^1) + (2 + 3^2) + (2 + 3^3) + (2 + 3^{11}) \\
&= (2 + 2 + 2 + \dots 11 \text{ times}) + (3 + 3^2 + 3^3 + \dots + 3^{11}) \\
&= 22 + (3 + 3^2 + 3^3 + \dots + 3^{11}) \dots \dots \dots (i)
\end{aligned}$$

Here  $3, 3^2, 3^3, \dots, 3^{11}$  is in G.P.

$$\therefore a = 3 \text{ and } r = \frac{3^2}{3} = 3$$

$$S_n = \frac{3(3^{11}-1)}{3-1} = \frac{3}{2}(3^{11}-1)$$

$$\text{Putting the value of } S_n \text{ in eq. (i), we get } \sum_{k=1}^{11} (2+3^k) = 22 + \frac{3}{2}(3^{11}-1)$$

31. Given,  $n(P) = 18$ ,  $n(C) = 23$ ,  $n(M) = 24$ ,  $n(C \cap M) = 13$ ,

$$n(P \cap C) = 12, n(P \cap M) = 11 \text{ and } n(P \cap C \cap M) = 6$$

i. Total no. of students in the class

$$\begin{aligned} &= n(P \cup C \cup M) \\ &= n(P) + n(C) + n(M) - n(P \cap C) - n(P \cap M) - n(C \cap M) + n(P \cap C \cap M) \\ &= 18 + 23 + 24 - 12 - 11 - 13 + 6 = 35 \end{aligned}$$

ii. No. of students who took Mathematics but not Chemistry

$$\begin{aligned} &= n(M - C) \\ &= n(M) - n(M \cap C) \\ &= 24 - 13 = 11 \end{aligned}$$

iii. No. of students who took exactly one of the three subjects

$$\begin{aligned} &= n(P) + n(C) + n(M) - 2n(M \cap P) - 2n(P \cap C) - 2n(M \cap C) + 3n(P \cap C \cap M) \\ &= 18 + 23 + 24 - 2 \times 11 - 2 \times 12 - 2 \times 13 + 3 \times 6 \\ &= 65 - 22 - 24 - 26 + 18 \\ &= 83 - 72 = 11 \end{aligned}$$

### Section D

32. We have

$$N = \sum_{i=1}^6 f_i = (6 + 8 + 15 + 3 + 8 + 4) = 44$$

$$\begin{aligned} \bar{x} &= \frac{\sum_{i=1}^6 f_i x_i}{N} = \frac{(6 \times 3) + (8 \times 5) + (15 \times 7) + (3 \times 9) + (8 \times 11) + (4 \times 13)}{44} \\ &= \frac{(18 + 40 + 105 + 27 + 88 + 52)}{44} = \frac{330}{44} = \frac{15}{2} = 7.5 \end{aligned}$$

$x_i$	3	5	7	9	11	13
$f_i$	6	8	15	3	8	4
cf	6	14	29	32	40	44

Here we have,  $N = 44$ , which is even.

$$\text{Therefore, median} = \frac{1}{2} \cdot \left\{ \frac{N}{2} \text{ th observation} + \left( \frac{N}{2} + 1 \right) \text{ th observation} \right\}$$

$$= \frac{1}{2} (22\text{nd observation} + 23\text{rd observation})$$

$$= \frac{1}{2} (7 + 7) = 7$$

Thus,  $M = 7$ .

Now, we have:

$ x_i - M $	4	2	0	2	4	6
$f_i$	6	8	15	3	8	4
$f_i  x_i - M $	24	16	0	6	32	24

$$\therefore \sum_{i=1}^6 f_i = 44 \text{ and } \sum_{i=1}^6 f_i |x_i - M| = 102$$

$$\therefore MD(\bar{x}) = \frac{\sum_{i=1}^6 f_i |x_i - M|}{N} = \frac{102}{44} = 2.32$$

33. Here, the equation of circle is  $x^2 + y^2 + 4x + 6y + 11 = 0$

$$\Rightarrow (x^2 + 4x) + (y^2 + 6y) = -11$$

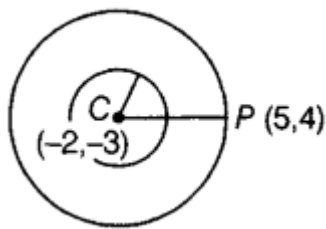
On adding 4 and 9 both sides to make perfect squares, we get

$$(x^2 + 4x + 4) + (y^2 + 6y + 9) = -11 + 4 + 9$$

$$\Rightarrow (x + 2)^2 + (y + 3)^2 = (\sqrt{2})^2 \dots(i)$$

Its centre is  $(-2, -3)$





The required circle is concentric with circle 1, therefore its centre is  $(-2, -3)$ . Since, it passes through  $(5, 4)$ , therefore radius is  $r = CP = \sqrt{(5+2)^2 + (4+3)^2}$  [ $\because$  distance  $= \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$ ]  
 $= \sqrt{49 + 49} = 7\sqrt{2}$

Hence, the equation of required circle having centre  $(-2, -3)$  and radius  $7\sqrt{2}$  is,

$$(x+2)^2 + (y+3)^2 = (7\sqrt{2})^2$$

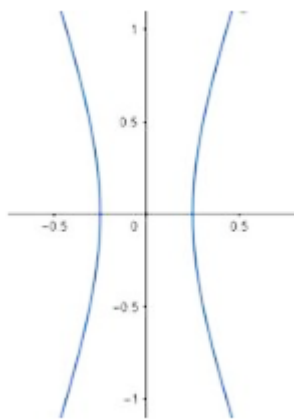
$$\Rightarrow x^2 + 4x + 4 + y^2 + 6y + 9 = 98$$

$$\Rightarrow x^2 + 4x + y^2 + 6y - 85 = 0$$

OR

Given: The length of latus rectum is 4, and the eccentricity is 3

Let, the equation of the hyperbola be:  $\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1$



The length of the latus rectum is 4 units.

$$\Rightarrow \text{length of the latus rectum} = \frac{2b^2}{a} = 4$$

$$\Rightarrow \frac{2b^2}{a} = 4 \Rightarrow b^2 = 2a \dots (i)$$

And also given, the eccentricity,  $e = 3$

$$\text{We know that, } e = \sqrt{1 + \frac{b^2}{a^2}}$$

$$\Rightarrow \sqrt{1 + \frac{b^2}{a^2}} = 3$$

$$\Rightarrow 1 + \frac{b^2}{a^2} = 9 \text{ [Squaring both sides]}$$

$$\Rightarrow \frac{b^2}{a^2} = 8$$

$$\Rightarrow b^2 = 8a^2$$

$$\Rightarrow 2a = 8a^2 \text{ [From (i)]}$$

$$\Rightarrow a = \frac{1}{4} \Rightarrow a^2 = \frac{1}{16}$$

$$\text{From (i)} \Rightarrow b^2 = 2a = 2 \times \frac{1}{4} = \frac{1}{2} \Rightarrow b^2 = \frac{1}{2}$$

So, the equation of the hyperbola is,

$$\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1 \Rightarrow \frac{x^2}{1/16} - \frac{y^2}{1/2} = 1$$

$$\Rightarrow 16x^2 - 2y^2 = 1$$

34. We have,  $\frac{4x}{3} - \frac{9}{4} < x + \frac{3}{4} \dots (i)$

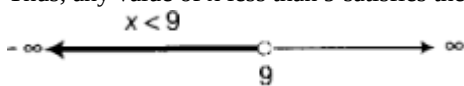
and  $\frac{7x-1}{3} - \frac{7x+2}{6} > x \dots (ii)$

From inequality (i), we get

$$\frac{4x}{3} - \frac{9}{4} < x + \frac{3}{4} \Rightarrow \frac{16x-27}{12} < \frac{4x+3}{4}$$

$$\begin{aligned} \Rightarrow 16x - 27 &< 12x + 9 \text{ [multiplying both sides by 12]} \\ \Rightarrow 16x - 27 + 27 &< 12x + 9 + 27 \text{ [adding 27 on both sides]} \\ \Rightarrow 16x &< 12x + 36 \\ \Rightarrow 16x - 12x &< 12x + 36 - 12x \text{ [ subtracting 12x from bot sides]} \\ \Rightarrow 4x &< 36 \Rightarrow x < 9 \text{ [dividing both sides by 4]} \end{aligned}$$

Thus, any value of  $x$  less than 9 satisfies the inequality. So, the solution of inequality (i) is given by  $x \in (-\infty, 9)$



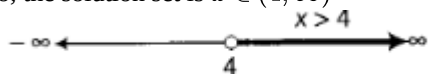
From inequality (ii) we get,

$$\begin{aligned} \frac{7x-1}{3} - \frac{7x+2}{6} > x &\Rightarrow \frac{14x-2-7x-2}{6} > x \\ \Rightarrow 7x - 4 &> 6x \text{ [multiplying by 6 on both sides]} \\ \Rightarrow 7x - 4 + 4 &> 6x + 4 \text{ [adding 4 on both sides]} \\ \Rightarrow 7x &> 6x + 4 \\ \Rightarrow 7x - 6x &> 6x + 4 - 6x \text{ [subtracting 6x from both sides]} \end{aligned}$$

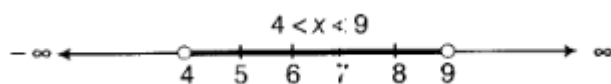
$$\therefore x > 4$$

Thus, any value of  $x$  greater than 4 satisfies the inequality.

So, the solution set is  $x \in (4, \infty)$



The solution set of inequalities (i) and (ii) are represented graphically on number line as given below:



Clearly, the common value of  $x$  lie between 4 and 9.

Hence, the solution of the given system is,  $4 < x < 9$  i.e.,  $x \in (4, 9)$

35. Given, LHS =  $\sin 20^\circ \sin 40^\circ \sin 80^\circ$

$$\begin{aligned} &= \frac{1}{2} [2 \sin 20^\circ \cdot \sin 40^\circ] \sin 80^\circ \text{ [multiplying and dividing by 2]} \\ &= \frac{1}{2} [\cos(20^\circ - 40^\circ) - \cos(20^\circ + 40^\circ)] \cdot \sin 80^\circ \text{ [}\therefore 2 \sin x \cdot \sin y = \cos(x - y) - \cos(x + y)\text{]} \\ &= \frac{1}{2} [\cos(-20^\circ) - \cos 60^\circ] \sin 80^\circ \\ &= \frac{1}{2} [\cos 20^\circ - \frac{1}{2}] \cdot \sin 80^\circ \text{ [}\therefore \cos(-\theta) = \cos \theta \text{ and } \cos 60^\circ = \frac{1}{2}\text{]} \\ &= \frac{1}{2} \times \frac{1}{2} [2(\cos 20^\circ - \frac{1}{2}) \cdot \sin 80^\circ] \text{ [again multiplying and dividing by 2]} \\ &= \frac{1}{4} [2 \cos 20^\circ \cdot \sin 80^\circ - \sin 80^\circ] \\ &= \frac{1}{4} [\sin(20^\circ + 80^\circ) - \sin(20^\circ - 80^\circ) - \sin 80^\circ] \text{ [}\therefore 2 \cos x \cdot \sin y = \sin(x + y) - \sin(x - y)\text{]} \\ &= \frac{1}{4} [\sin 100^\circ - \sin(-60^\circ) - \sin 80^\circ] \\ &= \frac{1}{4} [\sin 100^\circ + \sin 60^\circ - \sin 80^\circ] \text{ [}\therefore \sin(-\theta) = -\sin \theta\text{]} \\ &= \frac{1}{4} [\sin(180^\circ - 80^\circ) + \sin 60^\circ - \sin 80^\circ] \text{ [}\therefore \sin 100^\circ = \sin(180^\circ - 80^\circ)\text{]} \\ &= \frac{1}{4} [\sin 80^\circ + \sin 60^\circ - \sin 80^\circ] \text{ [}\therefore \sin(\pi - \theta) = \sin \theta\text{]} \\ &= \frac{1}{4} \times \sin 60^\circ = \frac{1}{4} \times \frac{\sqrt{3}}{2} \text{ [}\therefore \sin 60^\circ = \frac{\sqrt{3}}{2}\text{]} \\ &= \frac{\sqrt{3}}{8} = \text{RHS} \end{aligned}$$

Hence proved.

OR

$$\begin{aligned} \text{LHS} &= \cos 12^\circ + \cos 60^\circ + \cos 84^\circ \\ &= \cos 12^\circ + (\cos 84^\circ + \cos 60^\circ) \\ &= \cos 12^\circ + [2 \cos \left( \frac{84^\circ + 60^\circ}{2} \right) \times \cos \left( \frac{84^\circ - 60^\circ}{2} \right)] \\ &[\therefore \cos x + \cos y = 2 \cos \left( \frac{x+y}{2} \right) \cos \left( \frac{x-y}{2} \right)] \\ &= \cos 12^\circ + [2 \cos \frac{144^\circ}{2} \times \cos \frac{24^\circ}{2}] \\ &= \cos 12^\circ + [2 \cos 72^\circ \times \cos 12^\circ] = \cos 12^\circ [1 + 2 \cos 72^\circ] \\ &= \cos 12^\circ [1 + 2 \cos(90^\circ - 18^\circ)] \\ &= \cos 12^\circ [1 + 2 \sin 18^\circ] \text{ [}\therefore \cos(90^\circ - \theta) = \sin \theta\text{]} \\ &= \cos 12^\circ [1 + 2 \left( \frac{\sqrt{5}-1}{4} \right)] \text{ [}\therefore \sin 18^\circ = \frac{\sqrt{5}-1}{4}\text{]} \end{aligned}$$

$$= \left(1 + \frac{\sqrt{5}-1}{2}\right) \cos 12^\circ = \left(\frac{\sqrt{5}+1}{2}\right) \cos 12^\circ$$

$$\text{RHS} = \cos 24^\circ + \cos 48^\circ$$

$$= 2 \cos \left(\frac{24^\circ+48^\circ}{2}\right) \cos \left(\frac{24^\circ-48^\circ}{2}\right) \left[ \because \cos x + \cos y = 2 \cos \left(\frac{x+y}{2}\right) \cos \left(\frac{x-y}{2}\right) \right]$$

$$= 2 \cos 36^\circ \cos(-12^\circ)$$

$$= 2 \cos 36^\circ \times \cos 12^\circ \left[ \because \cos(-\theta) = \cos \theta \right]$$

$$= 2 \times \frac{\sqrt{5}+1}{4} \times \cos 12^\circ = \frac{\sqrt{5}+1}{2} \times \cos 12^\circ \left[ \because \cos 36^\circ = \frac{\sqrt{5}+1}{4} \right]$$

$\therefore \text{LHS} = \text{RHS}$

Hence proved.

### Section E

36. i. Number of functions from A to B are  $n(B)^{n(A)} = q^p$   
 ii. Number of relations from A to B is  $2^{n(A)n(B)} = 2^{pq}$ .  
 iii. Figures A and B show relations. Figure C shows a function but not a relation.

**OR**

x is a factor of y.

1, 2, 4 and 8 are factors of 8.

37. i. Total marbles =  $4 + 5 + 3 = 12$

$$\text{Required probability} = \frac{{}^4C_2}{{}^{12}C_2} = \frac{\frac{4 \times 3}{2 \times 1}}{\frac{12 \times 11}{2 \times 1}} = \frac{1}{11}$$

- ii. Total marbles =  $4 + 5 + 3 = 12$

$$\text{Required probability} = \frac{{}^3C_3}{{}^{12}C_3} = \frac{1}{\frac{12 \times 11 \times 10}{3 \times 2}} = \frac{1}{220}$$

- iii. Total marbles =  $4 + 5 + 3 = 12$

$$\text{Required probability} = \frac{{}^7C_2}{{}^{12}C_2} = \frac{\frac{7 \times 6}{2 \times 1}}{\frac{12 \times 11}{2 \times 1}} = \frac{21}{66} = \frac{7}{22}$$

**OR**

Total marbles =  $4 + 5 + 3 = 12$

Required probability =  $1 - P(\text{None is blue})$

$$= 1 - \frac{{}^7C_3}{{}^{12}C_3}$$

$$= 1 - \frac{\frac{7 \times 6 \times 5}{3 \times 2}}{\frac{12 \times 11 \times 10}{3 \times 2}}$$

$$= 1 - \frac{7}{44} = \frac{37}{44}$$

38. i.  $r = |Z| = 2\sqrt{2}$

$$x = 2, y = -2$$

$$\cos \theta = \frac{x}{r} = \frac{2}{2\sqrt{2}} = \frac{1}{\sqrt{2}}$$

$$\sin \theta = \frac{y}{r} = \frac{-2}{2\sqrt{2}} = \frac{-1}{\sqrt{2}}$$

$$\text{Arg}(Z) = \frac{-\pi}{4}$$

ii.  $z\bar{z} = |z|^2 = (2\sqrt{2})^2 = 8$

iii.  $|Z| = \sqrt{2^2 + (-2)^2}$

$$= \sqrt{8} = 2\sqrt{2}$$

**OR**

Real part of  $2 - 2i = 2$

